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Core Subject Area: Secondary II Mathematics

Mathematics, Secondary II

Standard	Designated Sections
Domain: Number	
Extend the properties of exponents to rational exponents.	
N.RN.1 Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. *For example, we define $5^{1/3}$ to be the cube root of 5 because we want $(5^{1/3})^3 = 5^{(1/3)3}$ to hold, so $(5^{1/3})^3$ must equal 5.*	Module 3 Task 1 Experimenting with Exponents Module 3 Task 2 Half Interested Module 3 Task 3 More Interesting Module 3 Task 4 Radical Ideas
N.RN.2 Rewrite expressions involving radicals and rational exponents using the properties of exponents.	Module 3 Task 3 More Interesting Module 3 Task 4 Radical Ideas
Use properties of rational and irrational numbers.	

N.RN.3 Explain why sums and products of rational numbers are rational, that the sum of a rational number and an irrational number is irrational, and that the product of a nonzero rational number and an irrational number is irrational.	Module 3 Task 9 My Irrational and Imaginary Friends Module 3 Task 10 iNumbers
Perform arithmetic operations with complex numbers.	
N.CN.1 Know there is a complex number i such that $i^2 = -1$, and every complex number has the form $a + bi$ with a and b real.	Module 3 Task 9 My Irrational and Imaginary Friends Module 3 Task 10 iNumbers
N.CN.2 Use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.	Module 3 Task 9 My Irrational and Imaginary Friends Module 3 Task 10 iNumbers
Use complex numbers in polynomial identities and equations.	
N.CN.7 Solve quadratic equations with real coefficients that have complex solutions.	Module 3 Task 8 To Be Determined Module 3 Task 9 My Irrational and Imaginary Friends
N.CN.8 Extend polynomial identities to the complex numbers. *For example, rewrite $x^2 + 4$ as $(x + 2i)(x - 2i)$.*	Module 3 Task 8 To Be Determined Module 3 Task 9 My Irrational and Imaginary Friends
N.CN.9 Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.	Module 3 Task 8 To Be Determined Module 3 Task 9 My Irrational and Imaginary Friends
Domain: Algebra	
Interpret the structure of expressions.	

A.SSE.1 Interpret expressions that represent a quantity in terms of its context.
 	
   a.   Interpret parts of an expression, such as terms, factors, and coefficients.
   b.   Interpret complicated expressions by viewing one or more of their parts as a single entity. *For example, interpret $P(1+r)^n$ as the product of P and a factor not depending on P.*
	Module 1 Task 1 Something to Talk About
	Module 1 Task 2 I Rule
	Module 1 Task 4 Rabbit Run
	Module 1 Task 5 Look Out Below
	Module 1 Task 6 Tortoise and Hare

A.SSE.2 Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$.	Module 2 Task 3 Building The Perfect Square Module 2 Task 4 Factor Fixin' Module 2 Task 5 Lining Up Quadratics
Write expressions in equivalent forms to solve problems.	

A.SSE.3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.⬚
 	
    a.   Factor a quadratic expression to reveal the zeros of the function it defines.
 	
    b. Complete the square in a quadratic expression to reveal the maxi- mum or minimum value of the function it defines.
    c. Use the properties of exponents to transform expressions for exponential functions. *For example the expression 1.15^t can be rewritten as $(1.15^{1/12})^{12t} \approx 1.012^{12t}$ to reveal the approximate equivalent monthly interest rate if the annual rate is 15%.*
	Module 2 Task 4 Factor Fixin'
	Module 2 Task 5 Lining Up Quadratics
	Module 2 Task 6 I've Got a Fill-in
	Module 3 Task 3 More Interesting

Perform arithmetic operations on polynomials.	
A.APR.1 Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.	Module 3 Task 10 iNumbers
Create equations that describe numbers or relationships.	
A.CED.1 Create equations and inequalities in one variable and use them to solve problems. *Include equations arising from linear and quadratic functions, and simple rational and exponential functions.*	Module 3 Task 6 Curbside Rivalry Module 3 Task 7 Perfecting My Quads Module 3 Task 11 Quadratic Quandaries
A.CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.	Module 1 Task 1 Something to Talk About Module 1 Task 2 I Rule Module 1 Task 4 Rabbit Run Module 1 Task 5 Look Out Below Module 1 Task 6 Tortoise and Hare
A.CED.4 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. *For example, rearrange Ohm's law V = IR to highlight resistance R.*	Module 3 Task 5 Throwing an Interception Module 3 Task 6 Curbside Rivalry Module 3 Task 7 Perfecting My Quads

Solve equations and inequalities in one variable.	
A.REI.4 Solve quadratic equations in one variable. [SEP] a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(x - p)^2 = q$ that has the same solutions. Derive the quadratic formula from this form. b. Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm bi$ for real numbers a and b.	Module 3 Task 5 Throwing an Interception Module 3 Task 6 Curbside Rivalry Module 3 Task 7 Perfecting My Quads Module 3 Task 8 To Be Determined
Solve systems of equations.	
A.REI.7 Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. *For example, find the points of intersection between the line y = –3x and the circle $x^2 + y^2 = 3$.*	Module 3 Task 6 Curbside Rivalry Module 3 Task 7 Perfecting My Quads
Domain: Function	
Interpret functions that arise in applications in terms of a context.	
F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. *Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.*	Module 4 Task 7 More Features, More Functions *This standard shows up as a related standard throughout many tasks in Modules 1, 2, 3, and 4.
F.IF.5 Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. *For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.* ★	Module 4 Task 1 Some of This, Some of That Module 4 Task 2 Bike Lovers Module 4 Task 2 Bike Lovers Module 4 Task 3 More Functions with Features Module 4 Task 4 Reflections of a Bike Lover
F.IF.6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. ★	Module 1 Task 5 Look Out Below Module 1 Task 6 Tortoise and the Hare Module 3 Task 1 Experimenting With Exponents
Analyze functions using different representations.	

F.IF.7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 	
  a. Graph linear and quadratic functions and show intercepts, maxima, and minima.
  b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
	Module 2 Task 1 Shifty y's
	Module 2 Task 2 Transformer's: More Than Meets the y's
	Module 4 Task 1 Some of This, Some of That
	Module 4 Task 2 Bike Lovers
	Module 4 Task 3 More Functions with Features
	Module 4 Task 4 Reflections of a Bike Lover

F.IF.8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.
 	
  a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.
  b. Use the properties of exponents to interpret expressions for exponential functions.
 	
    For example, identify percent rate of change in functions such as $y = (1.02)^t$, $y = (0.97)^t$, $y = (1.01)^{12t}$, $y = (1.2)^{t/10}$, and classify them as representing exponential growth or decay.
	Module 2 Task 3 Building the Perfect Square
	Module 2 Task 4 Factor Fixin'
	Module 2 Task 5 Lining Up Quadratics
	Module 2 Task 6 I've Got a Fill-in
	Module 3 Task 3 More Interesting

F.IF.9 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).	Module 1 Task 2 I Rule Module 1 Task 3 Scott's Macho March Module 1 Task 6 Tortoise and the Hare *This standard shows up as a related standard throughout many tasks in Modules 1, 2, 3, and 4.
Build a function that models a relationship between two quantities.	

F.BF.1 Write a function that describes a relationship between two quantities.*
 	
  a. Determine an explicit expression, a recursive process, or steps for calculation from a context.
  b. Combine standard function types using arithmetic operations. *For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model.*
	Module 1 Task 1 Something to Talk About
	Module 1 Task 2 I Rule
	Module 1 Task 3 Scott's Macho March
	Module 1 Task 4 Rabbit Run
	Module 1 Task 5 Look Out Below
	Module 1 Task 6 Tortoise and Hare
	Module 2 Task 4 Factor Fixin'
	Module 2 Task 5 Lining Up Quadratics
	Module 2 Task 6 I've Got a Fill-in

Build new functions from existing functions.	
F.BF.3 Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k\,f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. *Include recognizing even and odd functions from their graphs and algebraic expressions for them.*	Module 2 Task 1 Shifty y's Module 2 Task 2 Transformer's: More Than Meets the y's

F.BF.4 Find inverse functions.
   a. Solve an equation of the form $f(x) = c$ for a simple function f that has an inverse and write an expression for the inverse. *For example, $f(x) = 2\,x^3$ or $f(x) = (x+1)/(x-1)$ for x* $\neq$*1. c. (+) Read values of an inverse function from a graph or a table, given that the function has an inverse.*
   d. *(+) Produce an invertible function from a non-invertible function by restricting the domain.*
	Module 4 Task 5 What's Your Pace?
	Module 4 Task 6 Bernie's Bikes

Construct and compare linear, quadratic, and exponential models and solve problems.	
F.LE.3 Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.	Module 1 Task 3 Scott's Macho March Module 1 Task 6 Tortoise and Hare Module 1 Task 7 How does it Grow?
Prove and apply trigonometric identities.	
F.TF.8 Prove the Pythagorean identity $\sin^2(\theta) + \cos^2(\theta) = 1$ and use it to find $\sin(\theta)$, $\cos(\theta)$, or $\tan(\theta)$, given $\sin(\theta)$, $\cos(\theta)$, or $\tan(\theta)$, and the quadrant of the angle.	Module 6 Task 9 Relationships with Meaning Module 6 Task 11 Solving Right Triangles Using Trigonometric Relationships
Domain: Geometry	
Prove geometric theorems.	
G.CO.9 Prove theorems about lines and angles. *Theorems include: verti- cal angles are congruent; when a transversal crosses parallel lines, alter- nate interior angles are congruent and corresponding angles are con- gruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.*	Module 5 Task 2 Do You See What I See? Module 5 Task 3 It's All in Your Head Module 5 Task 4 Parallelism Preserved Module 5 Task 5 Conjectures and Proof Module 6 Task 5 Measured Reasoning
G.CO.10 Prove theorems about triangles. *Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.*	Module 5 Task 1 How Do You Know That? Module 5 Task 2 Do You See What I See? Module 5 Task 3 It's All in Your Head Module 5 Task 5 Conjectures and Proof

	Module 5 Task 8 Centers of a Triangle
	Module 6 Task 5 Measured Reasoning
G.CO.11 Prove theorems about parallelograms. *Theorems include: op- posite sides are congruent, opposite angles are congruent, the diago- nals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.*	Module 5 Task 2 Do You See What I See?
	Module 5 Task 6 Parallelogram Conjectures and Proof
	Module 5 Task 7 Guess My Parallelogram

Understand similarity in terms of similarity transformations.

G.SRT.1 Verify experimentally the properties of dilations given by a center and a scale factor.
 	
   a.   A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged.
   b.   The dilation of a line segment is longer or shorter in the ratio given by the scale factor.
	Module 6 Task 1 Photocopy Faux Pas

G.SRT.2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.	Module 6 Task 2 Triangle Dilations Module 6 Task 3 Similar Triangles and Other Figures
G.SRT.3 Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar.	Module 6 Task 3 Similar Triangles and Other Figures

Prove theorems involving similarity.

G.SRT.4 Prove theorems about triangles. *Theorems include: a line par- allel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.*	Module 6 Task 4 Cut By A Transversal Module 6 Task 5 Measured Reasoning Module 6 Task 7 Pythagoras By Proportions
G.SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figure	Module 6 Task 2 Triangle Dilations Module 6 Task 5 Measured Reasoning Module 6 Task 7 Pythagoras By Proportions

Define trigonometric ratios and solve problems involving right triangles.

G.SRT.6 Understand that by similarity, side ratios in right triangles are properties of the	Module 6 Task 8 Are Relationships Predictable?

angles in the triangle, leading to definitions of trigonometric ratios for acute angles.	Module 6 Task 9 Relationships with Meaning Module 6 Task 11 Solving Right Triangles Using Trigonometric Relationships
G.SRT.7 Explain and use the relationship between the sine and cosine of complementary angles.	Module 6 Task 9 Relationships with Meaning Module 6 Task 10 Finding the Value of a Relationship Module 6 Task 11 Solving Right Triangles Using Trigonometric Relationships
G.SRT.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.	Module 6 Task 8 Are Relationships Predictable? Module 6 Task 10 Finding the Value of a Relationship
Understand and apply theorems about circles.	
G.C.1 Prove that all circles are similar.	Module 7 Task 2 Circle Dilations
G.C.2 Identify and describe relationships among inscribed angles, radii, and chords. *Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.*	Module 7 Task 1 Centered Module 7 Task 3 Cyclic Polygons Module 7 Task 6 Circular Reasoning
G.C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.	Module 7 Task 3 Cyclic Polygons
G.C.4 Construct a tangent line from a point outside a given circle to the circle.	Module 7 Task 3 Cyclic Polygons
Find arc lengths and areas of sectors of circles.	
G.C.5 Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.	Module 7 Task 7 Pied Module 7 Task 8 Madison's Round Garden Module 7 Task 9 Rays and Radians
Translate between the geometric description and the equation for a conic section.	
G.GPE.1 Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.	Module 8 Task 1 Circling Triangles Module 8 Task 2 Getting Centered Module 8 Task 3 Circe Challenges
G.GPE.2 Derive the equation of a parabola given a focus and directrix.	Module 8 Task 4 Directing Our Focus Module 8 Task 5 Functioning with Parabolas Module 8 Task 6 Turn It Around
Use coordinates to prove simple geometric theorems algebraically.	

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically. *For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point (1, √3) lies on the circle centered at the origin and containing the point (0, 2).*	Module 8 Task 1 Circling Triangles (Or Triangulating Circles) Module 8 Task 2 Getting Centered Module 8 Task 3 Circle Challenges
G.GPE.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio.	Module 6 Task 6 Yard Work in Segments

Explain volume formulas and use them to solve problems.

G.GMD.1 Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. *Use dissection arguments, Cavalieri's principle, and informal limit arguments.*	Module 7 Task 4 Planning the Gazebo Module 7 Task 5 From Polygons to Circles Module 7 Task 10 Sand Castles
G.GMD.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.	Module 7 Task 10 Sand Castles

Domain: Statistics

Understand independence and conditional probability and use them to interpret data.

S.CP.1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").	Module 9 Task 3 Fried Freddy's *S.CP.1 is a related standard in several tasks throughout Module 9
S.CP.2 Understand that two events *A* and *B* are independent if the probability of *A* and *B* occurring together is the product of their probabilities, and use this characterization to determine if they are independent.	Module 9 Task 3 Fried Freddy's Module 9 Task 5 Freddy Revisited Module 9 Task 6 Striving for Independence
S.CP.3 Understand the conditional probability of *A* given *B* as *P(A and B)/P(B)*, and interpret independence of *A* and *B* as saying that the conditional probability of *A* given *B* is the same as the probability of *A*, and the conditional probability of *B* given *A* is the same as the probability of *B*.	Module 9 Task 5 Freddy Revisited Module 9 Task 6 Striving for Independence
S.CP.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. *For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results.*	Module 9 Task 2 Chocolate vs Vanilla Module 9 Task 5 Freddy Revisited Module 9 Task 6 Striving for Independence
S.CP.5 Recognize and explain the concepts of conditional probability and independence in	Module 9 Task 5 Freddy Revisited

everyday language and everyday situations. *For ex- ample, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer.*	Module 9 Task 6 Striving for Independence
Use the rules of probability to compute probabilities of compound events in a uniform probability model.	
S.CP.6 Find the conditional probability of *A* given *B* as the fraction of *B*'s outcomes that also belong to *A*, and interpret the answer in terms of the model.	Module 9 Task 1 TB or Not TB Module 9 Task 2 Chocolate vs Vanilla Module 9 Task 3 Fried Freddy's Module 9 Task 4 Visualizing with Venn Module 9 Task 6 Striving for Independence
S.CP.7 Apply the Addition Rule, *P(A or B) = P(A) + P(B) – P(A and B)*, and interpret the answer in terms of the model.	Module 9 Task 3 Fried Freddy's Module 9 Task 4 Visualizing with Venn
S.CP.8 (+) Apply the general Multiplication Rule in a uniform probability model, *P(A and B) = P(A)P(B|A) = P(B)P(A|B)*, and interpret the answer in terms of the model.	Module 9 Task 6 Striving for Independence